
Neutron diffraction

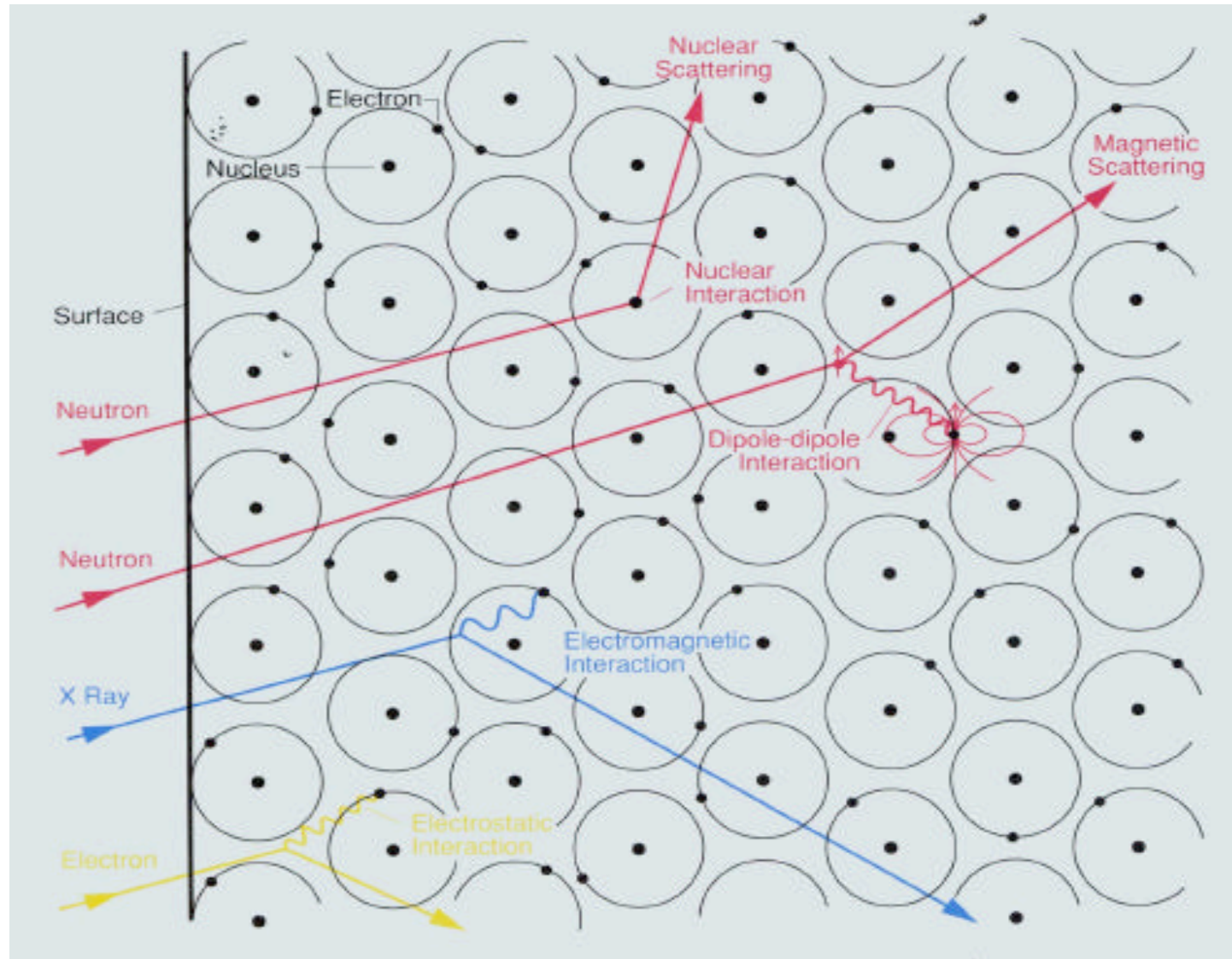


AMES LABORATORY

Rob McQueeney

IOWA STATE
UNIVERSITY

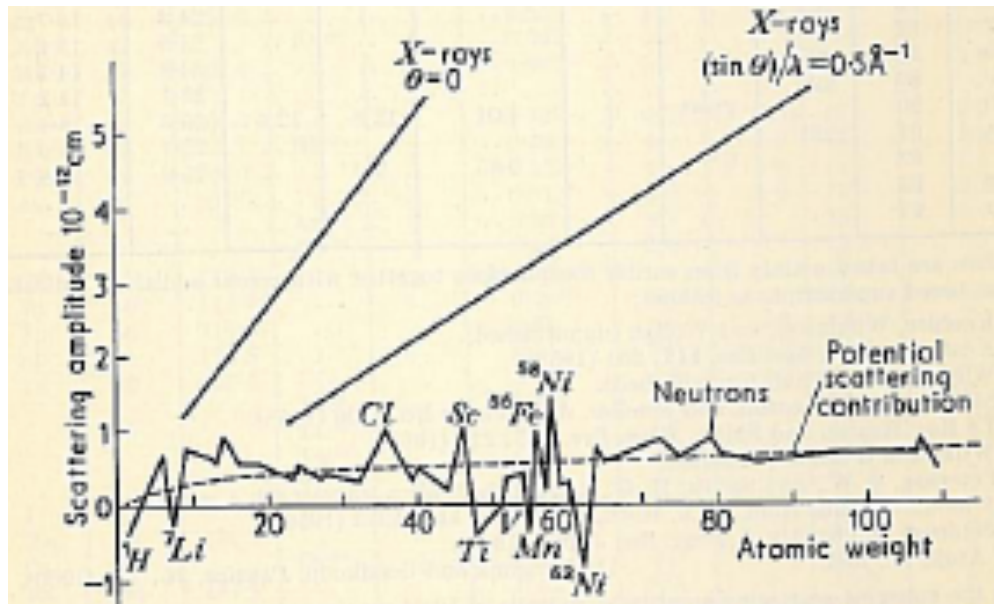
Different probes



Different probes

	NEUTRONS	X-RAYS	ELECTRONS
Wavelength range	0.4 - 10 Å	0.1 - 5 Å	0.04 - 0.2 Å
Energy range	0.001 - 0.5 eV	3000 - 100000 eV	6000 - 120000 eV
Cross-section	10^{-25} barns	$10^{-25} Z^2$ barns	$\sim 10^{-22}$ barns
Penetration depth	\sim cm	\sim μm	\sim nm
Typical flux	$10^{11} \text{ s}^{-1} \text{ m}^{-2}$	$10^{24} \text{ s}^{-1} \text{ m}^{-2}$	$10^{26} \text{ s}^{-1} \text{ m}^{-2}$
Beam size	mm-cm	μm -mm	nm- μm
Typical sample	Any bulk sample	Small crystals, powders, surfaces	Surfaces, thin films, grains, gases
Techniques	Diffraction Inelastic scattering Reflectivity	Diffraction Photon absorption Photoemission Inelastic scattering	Microscopy Diffraction Emission spectroscopy EELS
Phenomena	Magnetic/crystal structures collective excitations (phonons, spin waves) electronic excitations (crystal-field, spin-orbit)	Crystal structures, electronic transitions (photoemission, absorption),	microstructure crystal structures electronic transitions

Neutron cross-section



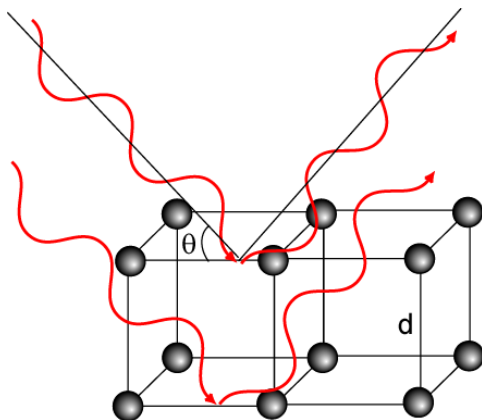
- **Nuclear property**
 - Random with Z
 - Depends on isotope
 - Depends on nuclear spin
 - Absorption can be problem

Phy

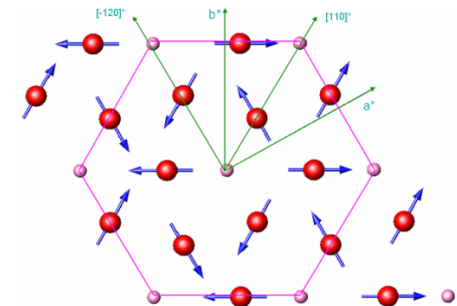
	Abundance (%)	Cross-section (bn)	Absorption (bn)
Gd	---	180	49700
152Gd	0.2	13	735
154Gd	2.1	13	85
155Gd	14.8	66	61100
156Gd	20.6	5	1.5
157Gd	15.7	1044	259000
158Gd	24.8	10	2.2
160Gd	21.8	10.52	0.77

Why neutrons??

- Penetration ~ centimeters, bulk probe
- Sensitivity to low-Z
- Isotopic contrast
- Wavelength range ~ interatomic spacing (1-2 Å) → diffraction
 - interacts with nuclei
 - Interacts with magnetic moment of unpaired e⁻
- Can measure crystal and magnetic structures



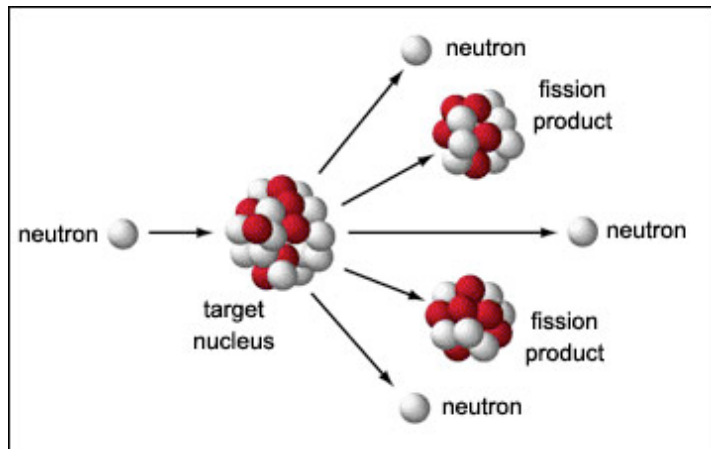
Elastic scattering - Bragg's Law
 $2d\sin\theta = n\lambda$



Producing neutrons

Fission

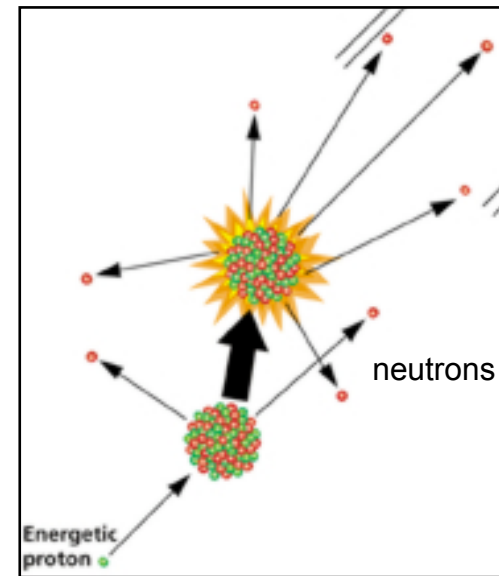
Nuclear reactor



Moderators → Cold-Thermal

Spallation

Particle accelerator

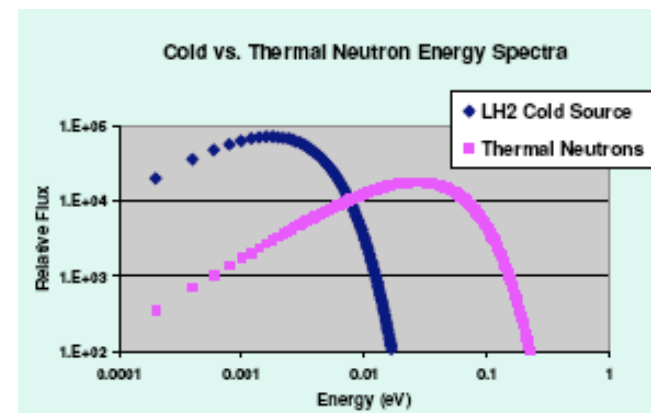
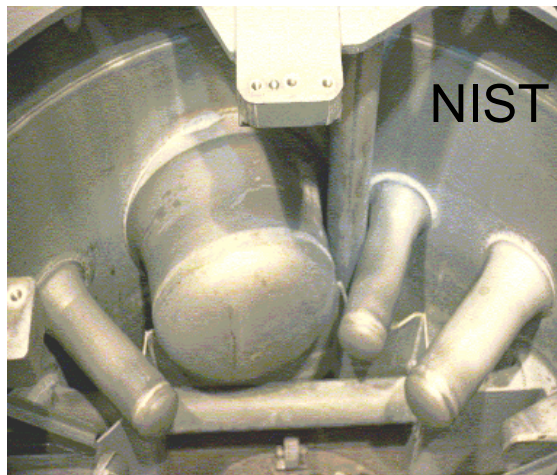
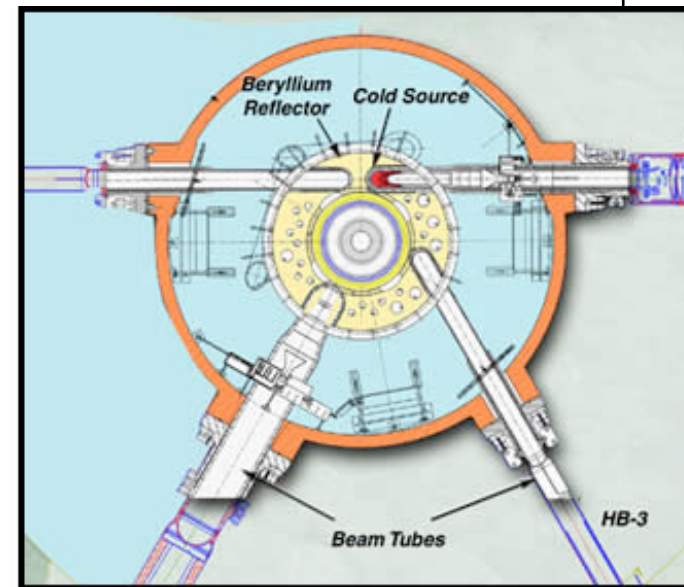


Moderators → Cold-Epithermal

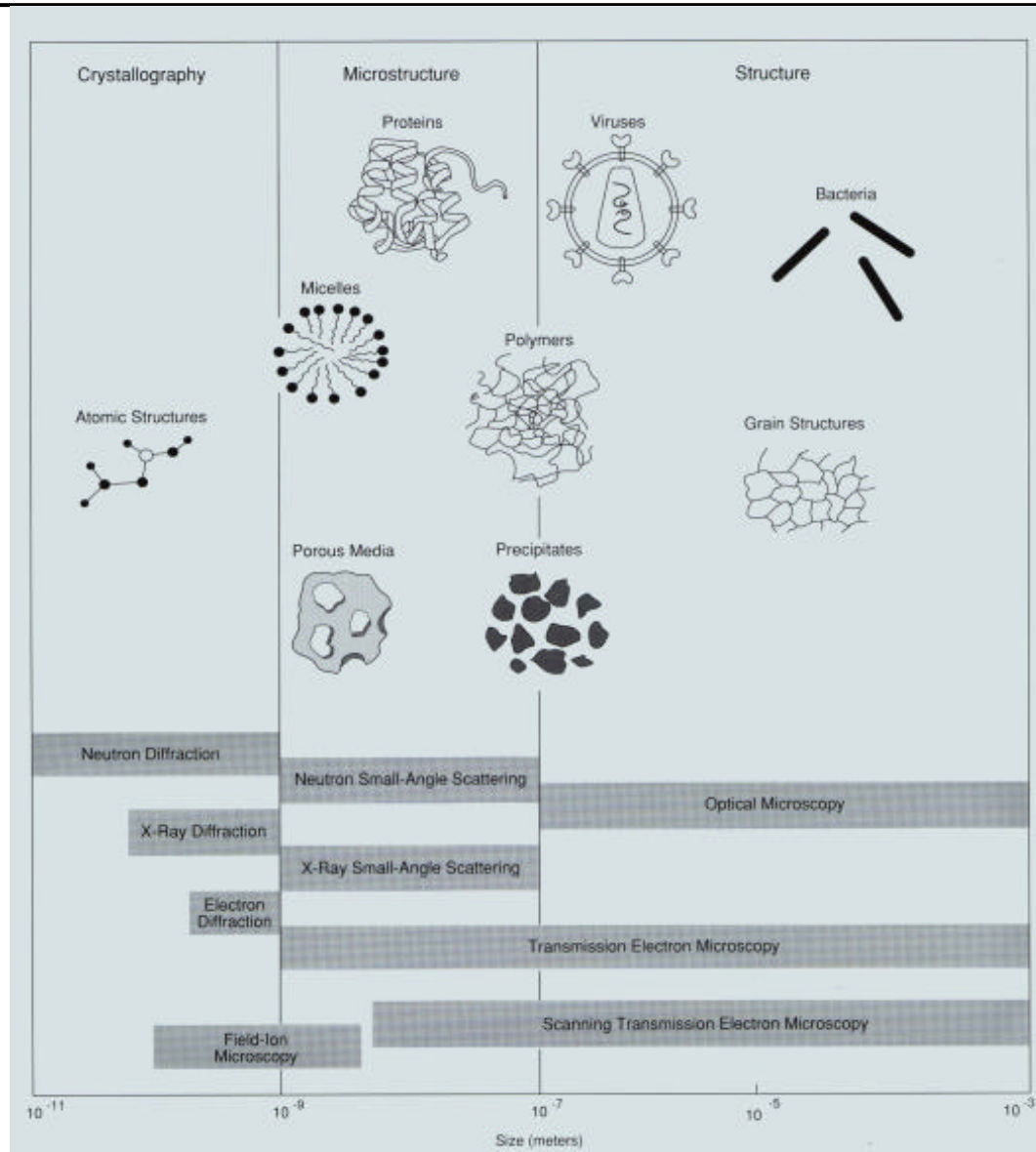
Neutrons by reactor fission



High flux isotope reactor - ORNL



Length scales

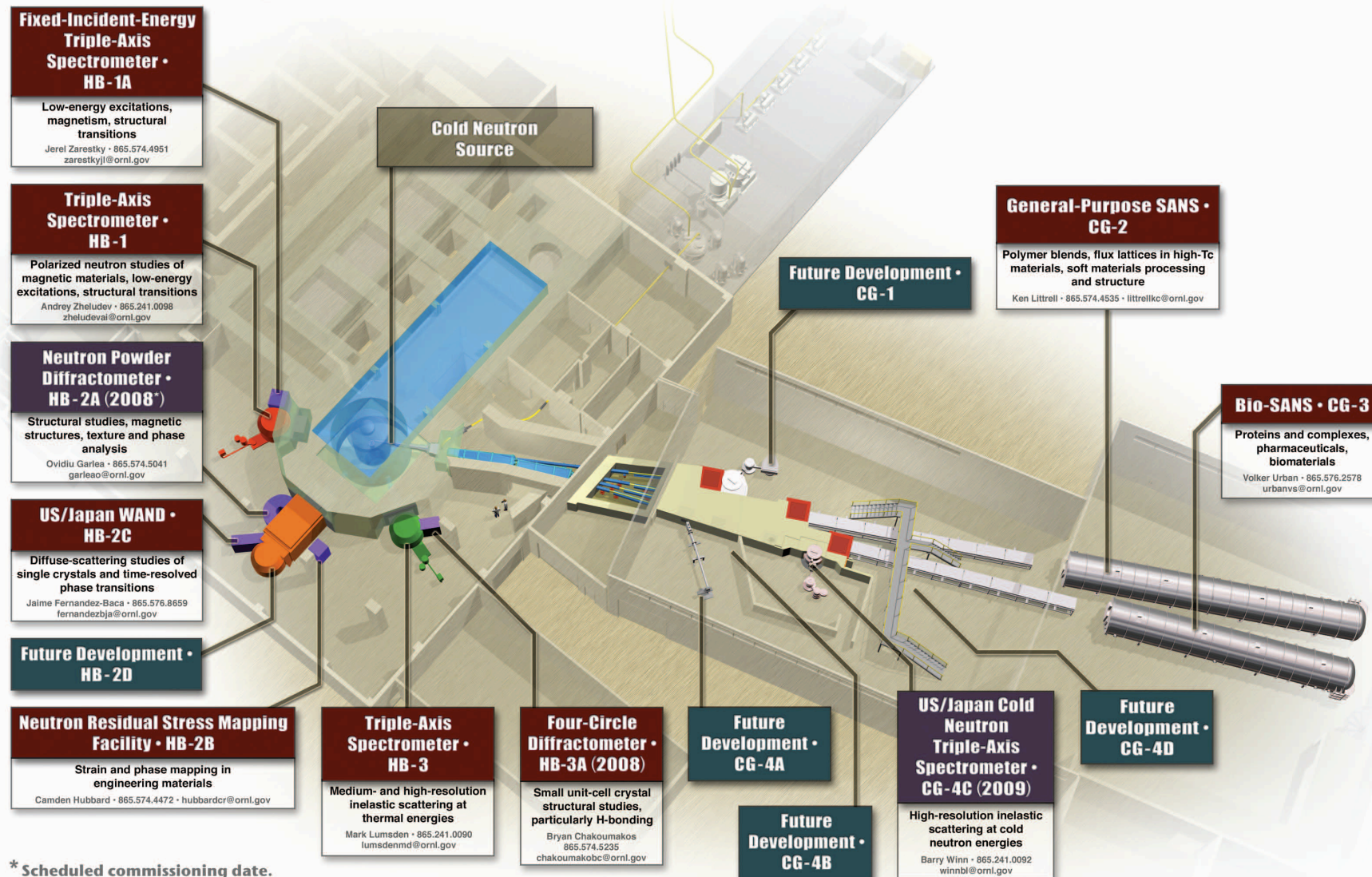


High Flux Isotope Reactor at Oak Ridge National Laboratory

The United States' highest flux reactor-based source of neutrons for condensed matter research



ORY



* Scheduled commissioning date.

LEGEND

- Installed, commissioning, or operating
- In design or construction
- Under consideration

07-G00244E/arm



NEUTRONS.ORNL.GOV

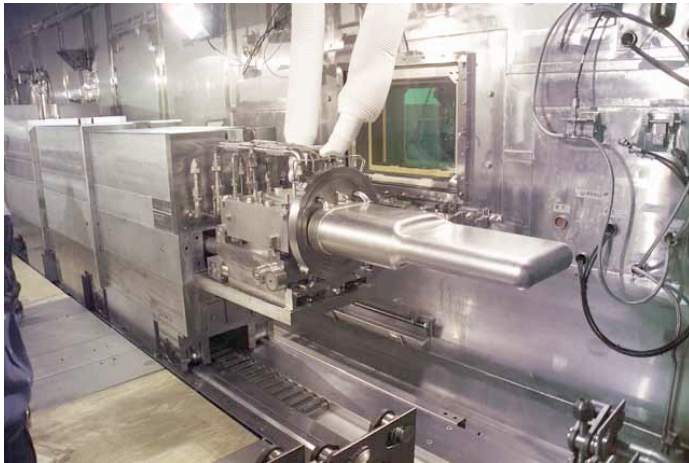
NEUTRON SCIENCES

Neutrons by pulsed spallation



Spallation Neutron Source (ORNL)

Target-moderator system



SNS liquid Hg target

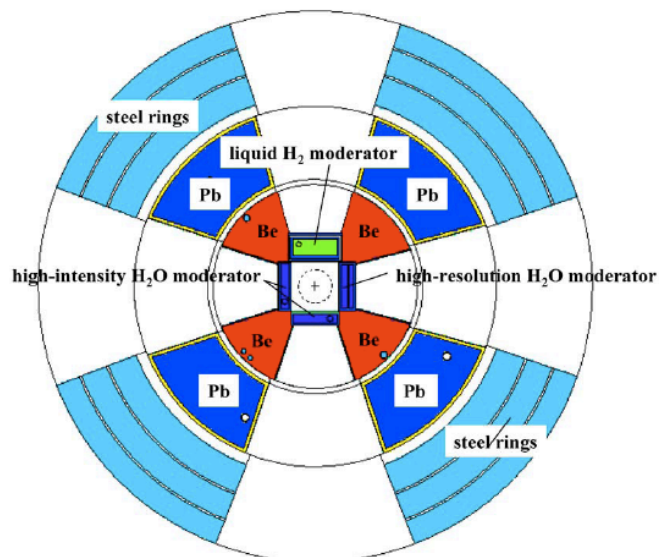
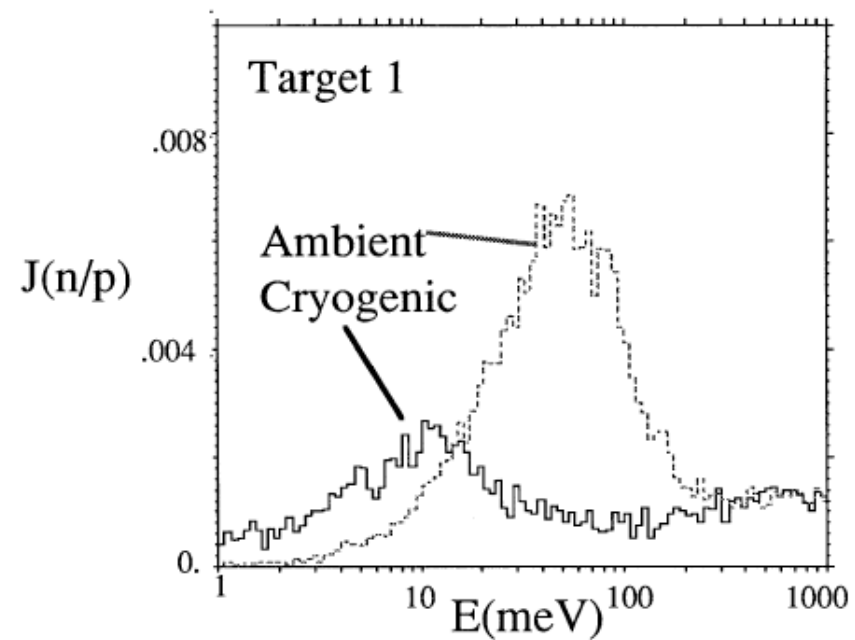


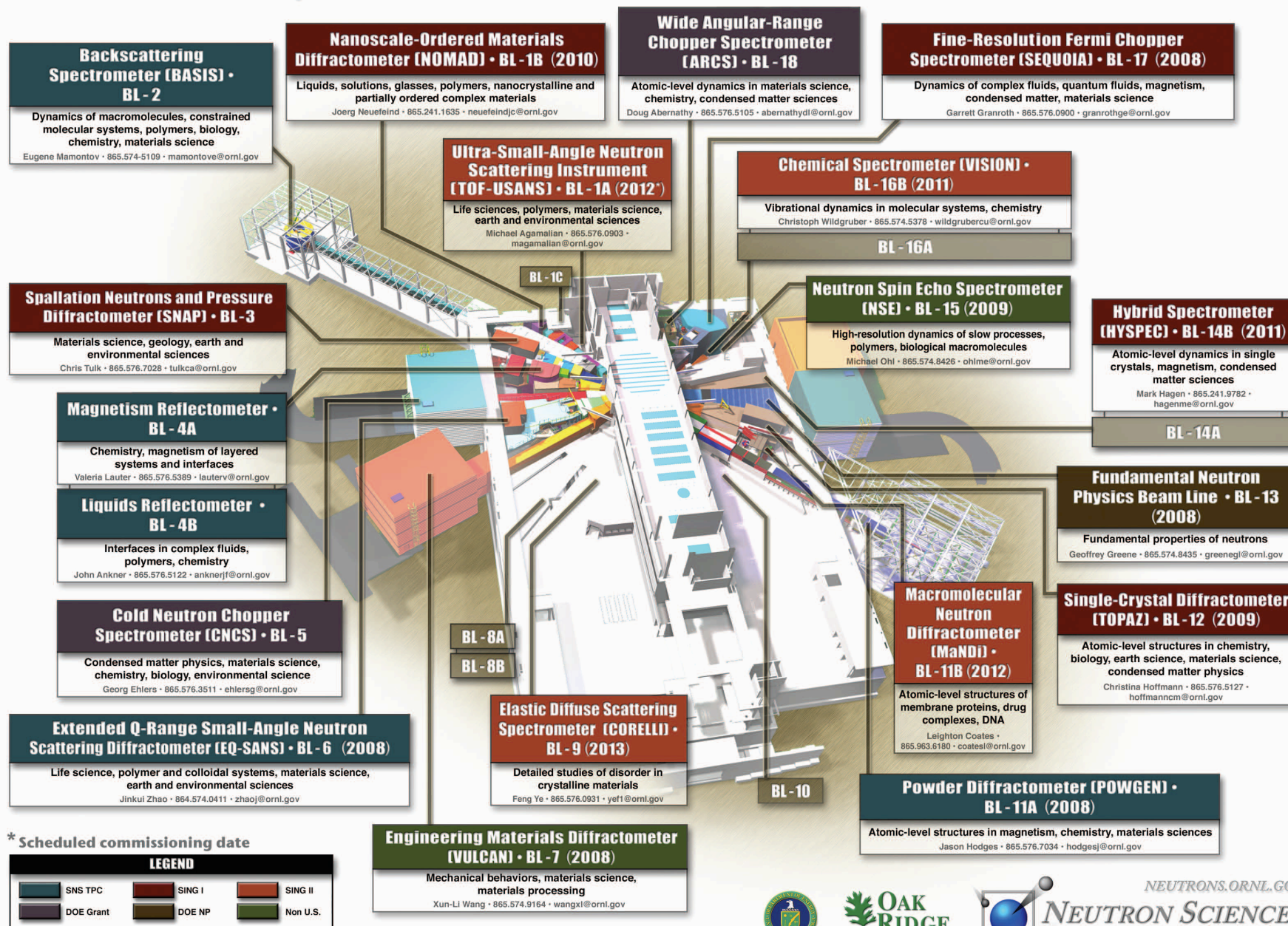
Fig. 3. Horizontal cross-section of the flux-trap moderators.



Spallation Neutron Source at Oak Ridge National Laboratory



The world's most intense pulsed, accelerator-based neutron source



* Scheduled commissioning date

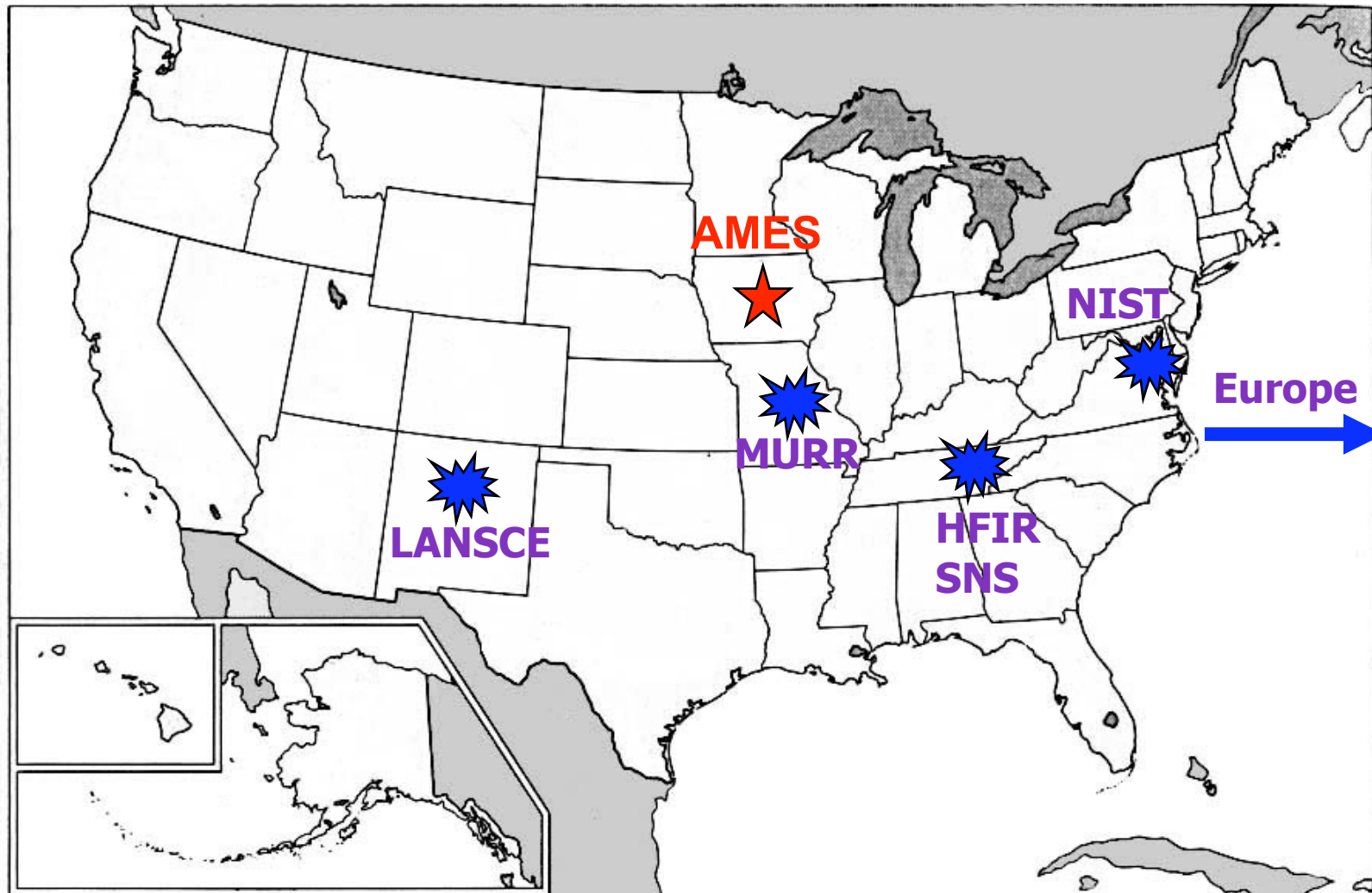
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NEUTRON SCIENCES

Places to go

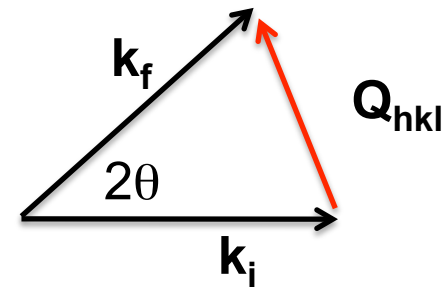


Powder diffraction

For single-crystal: $\mathbf{Q}_{hkl} = \mathbf{k}_f - \mathbf{k}_i$

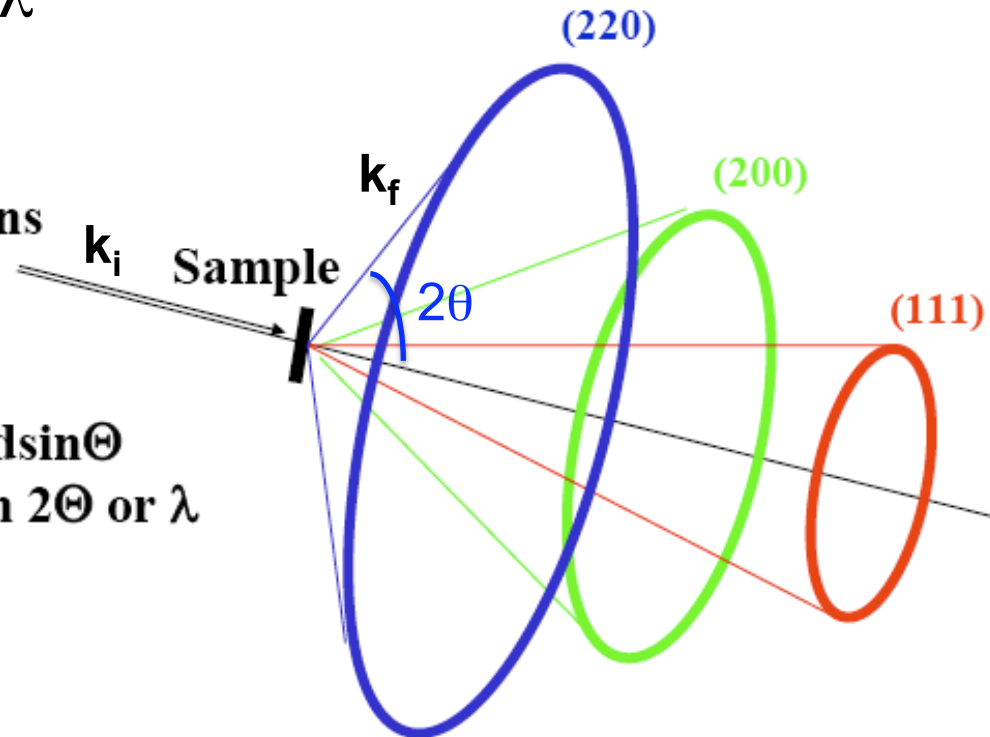
For powder: $Q_{hkl} = 2k_i \sin\theta$

$$k_i = 2\pi/\lambda$$



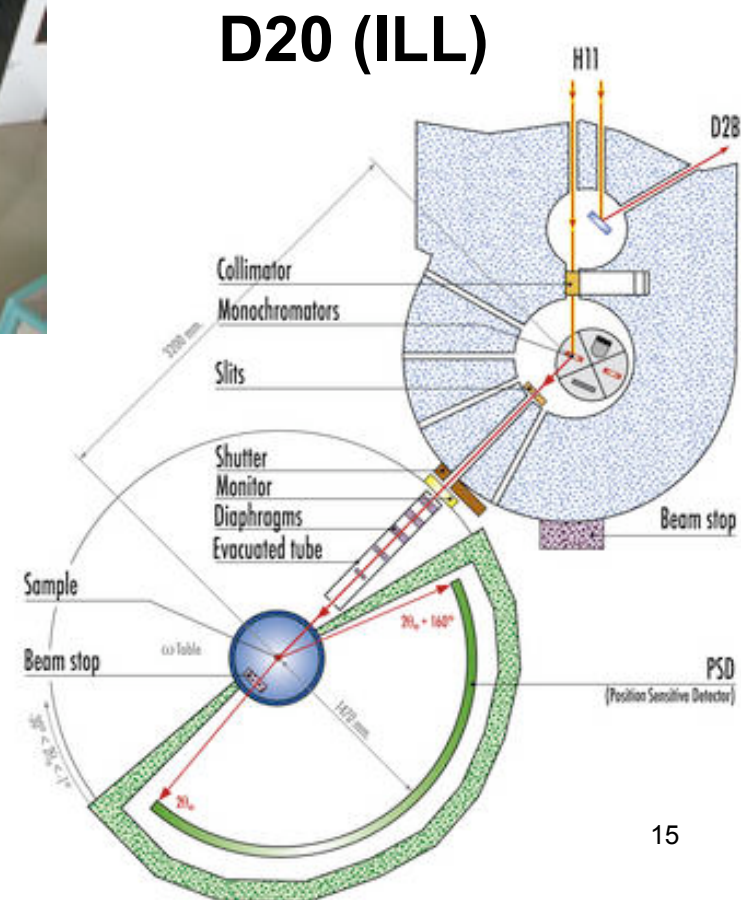
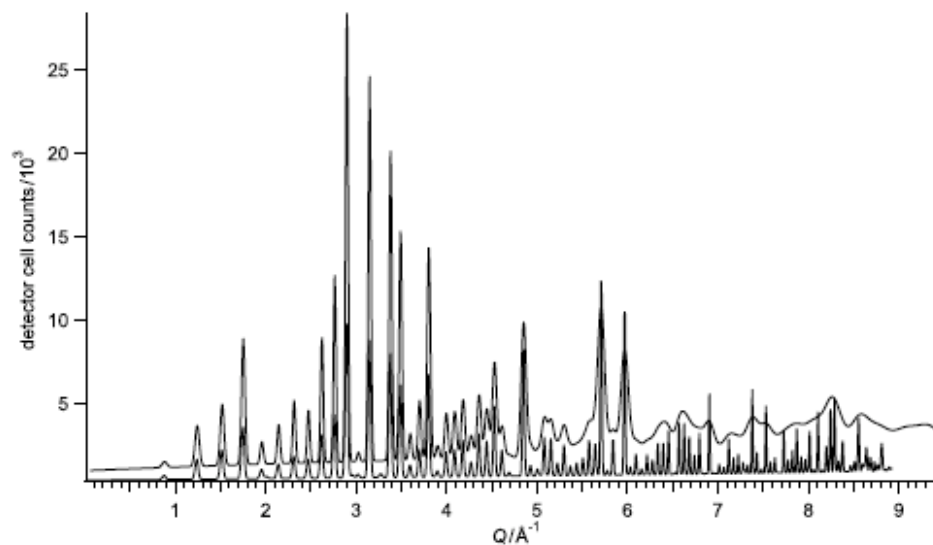
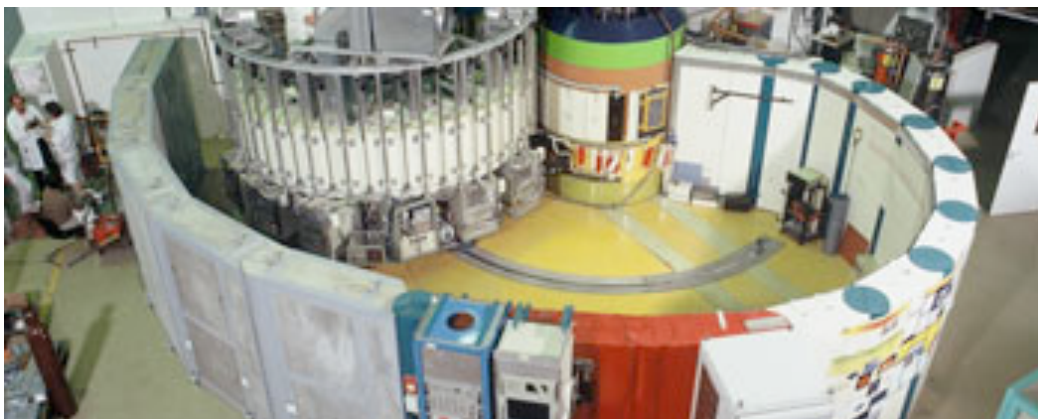
Incident beam
x-rays or neutrons

Bragg's Law $\lambda = 2d \sin\Theta$
Powder pattern – scan 2Θ or λ

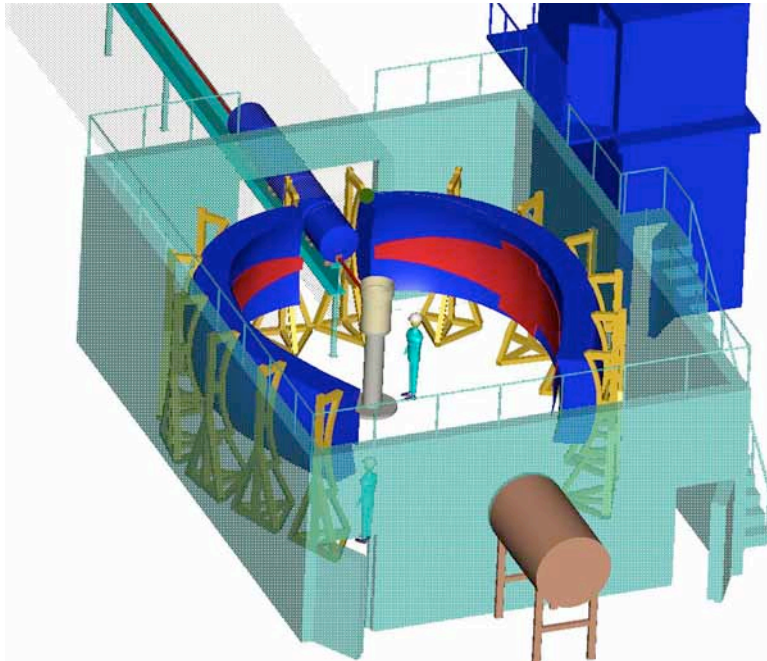


Powder diffraction

Determine the crystal structure



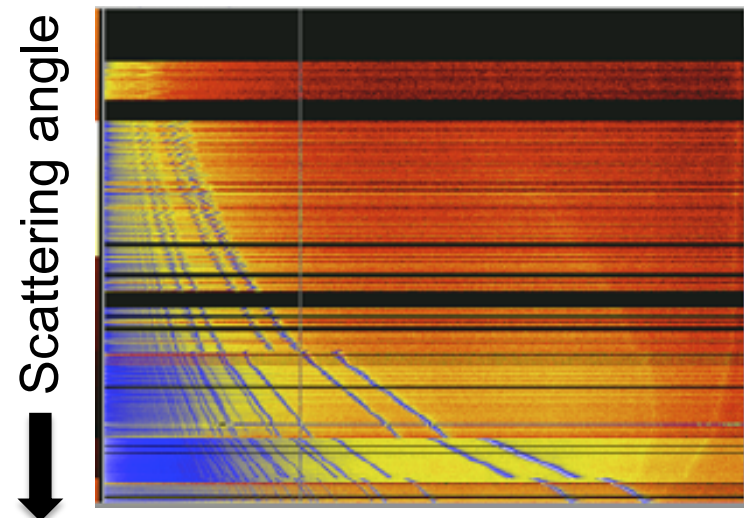
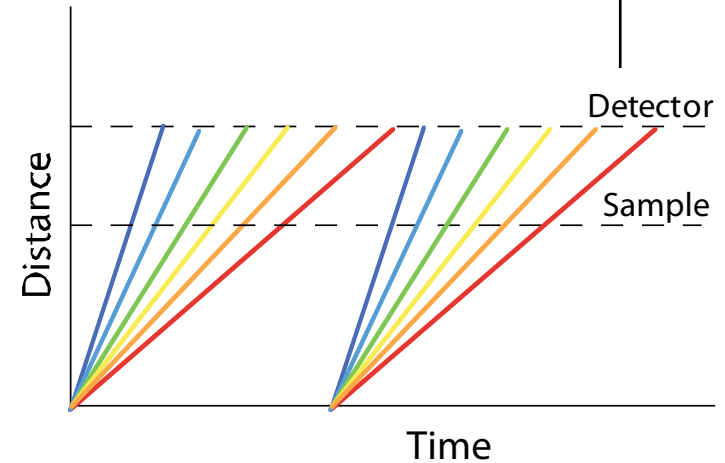
TOF powder diffraction



POWGEN @ SNS

Time-of-flight
$$\tau = L/v = \lambda m L/h = 2mLd \sin\theta/h$$

Physics 590



Time, wavelength, or d-spacing

Fitting diffraction data

• Rietveld refinement

- Lattice constants
- space group
- Atom positions
- Site disorder/vacancies
- Thermal vibration amplitude
- Strain broadening
- R-factor

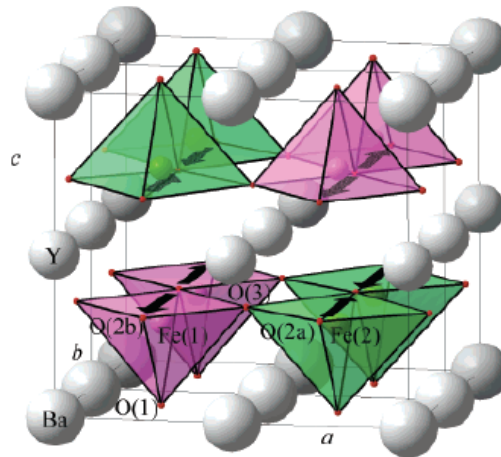


Figure 3. Crystal and magnetic structure of the class-I MV (charge-ordered) YBaFe_2O_5 at 20 K. Magnetic unit cell ($a \times 2b \times c$) is drawn.

Table 4. YBaFe_2O_5 Structure Refinement Results from NPD Data

T (K):	20	280	300	320	340
λ (Å)	1.5402	2.0783	2.0783	2.0783	2.0783
R_{wp}	0.0671	0.0789	0.0907	0.0783	0.0748
χ^2	4.78	1.38	1.91	1.25	1.17
space group	$Pmma^a$	$Pmma^a$	$Pmma^a$	$Pmmn^b$	$Pmmn^b$
a (Å)	8.0251(1)	8.0162(2)	8.0141(2)	3.93329(7)	3.93181(7)
b (Å)	3.83834(6)	3.85238(7)	3.85511(9)	3.91342(7)	3.91717(7)
c (Å)	7.5312(1)	7.5541(2)	7.5577(2)	7.5652(1)	7.5683(1)
a_1-b_1 (Å) ^c	0.1742	0.1557	0.1520	0.0199	0.0146
V (Å ³)	231.983(8)	233.28(1)	233.49(1)	116.447(5)	116.563(5)
Fe(1) z	0.2542(4)	0.2568(9)	0.257(1)	0.2640(2)	0.2641(2)
Fe(2) z	0.2695(4)	0.2662(9)	0.265(1)		
O(1) z	0.003(1)	0.001(3)	0.000(3)	0	0
O(2a) z	0.3213(7)	0.324(2)	0.325(2)	0.3137(5)	0.3140(6)
O(2b) z	0.3132(7)	0.307(2)	0.308(2)		
O(3) x	0.0098(7)	0.012(1)	0.011(2)	0	0
O(3) z	0.3119(3)	0.3130(4)	0.3115(4)	0.3127(5)	0.3125(6)
Y U_{iso} (Å ²)	0.0063(4)	0.0123(9)	0.013(1)	0.0152(8)	0.0137(7)
Ba U_{iso} (Å ²)	0.0039(6)	0.014(1)	0.017(1)	0.017(1)	0.0144(9)
Fe U_{iso}/U_{eqv} (Å ²) ^{d,e}	0.0039(3)	0.0124(6)	0.0139(8)	0.0132	0.0122
O(1) U_{eqv} (Å ²) ^d	0.0080	0.0138	0.0159	0.0181	0.0136
O(2) U_{eqv} (Å ²) ^{d,f}	0.0065	0.0123	0.0129	0.0186	0.0188
O(3) U_{eqv} (Å ²) ^d	0.0078	0.0128	0.0141	0.0146	0.0138
Fe M_y (μ_B)	3.82(2)	3.41(3)	3.26(3)	2.88(2)	2.76(2)
Fe M_z (μ_B)	0	0	0	-0.17(8)	-0.20(8)
Fe M_{Total} (μ_B)	3.82(2)	3.41(3)	3.26(3)	2.89(2)	2.77(2)

^a Wyckoff positions for space group $Pmma$ (nuclear cell) are: Ba at 2a (0,0,0); Y at 2c (0,0,1/2); Fe(1) and O(1) at 2f (1/4,1/2,z); Fe(2) at 2f (3/4,1/2,z); O(2a) at 2e (3/4,0,z); O(2b) at 2e (1/4,0,z); O(3) at 4j (x,1/2,z).

^b Wyckoff positions for space group $Pmmn$ (nuclear cell) are: Ba at 1a (0,0,0); Y at 1c (0,0,1/2); Fe at 2t (1/2,1/2,z); O(1) at 1f (1/2,1/2,0); O(2) at 2s (1/2,0,z); O(3) at 2r (0,1/2,z). ^c Orthorhombic distortion; refers to the single-perovskite-type subcell. ^d U_{eqv} values are given for those atoms where anisotropic displacement parameters were used in the refinement. The U_{eqv} values are defined as one-third the trace of the diagonal matrix describing the shape of the thermal ellipsoid. A complete list of the anisotropic displacement parameters is given in the Supporting Information. ^e The displacement parameters for Fe(1) and Fe(2) were constrained to be equal. An isotropic displacement parameter was used in the charge-ordered state; anisotropic displacement parameters were used for the MV state. ^f The displacement parameters for O(2a) and O(2b) were constrained to be equal.

Caution !!!

Things to keep in mind about powder diffraction measurements

- Easy to do, but make sure you have a good powder!!!

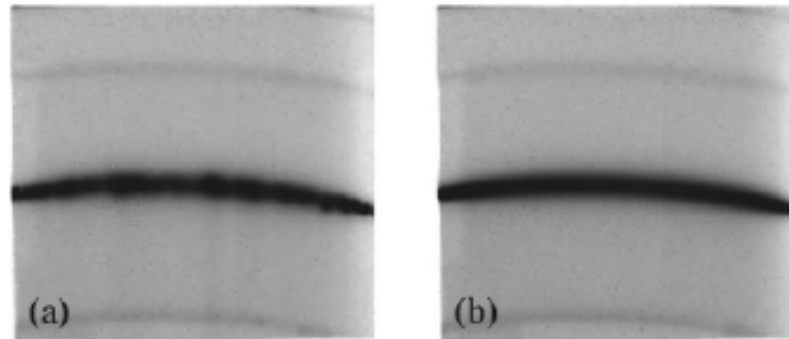
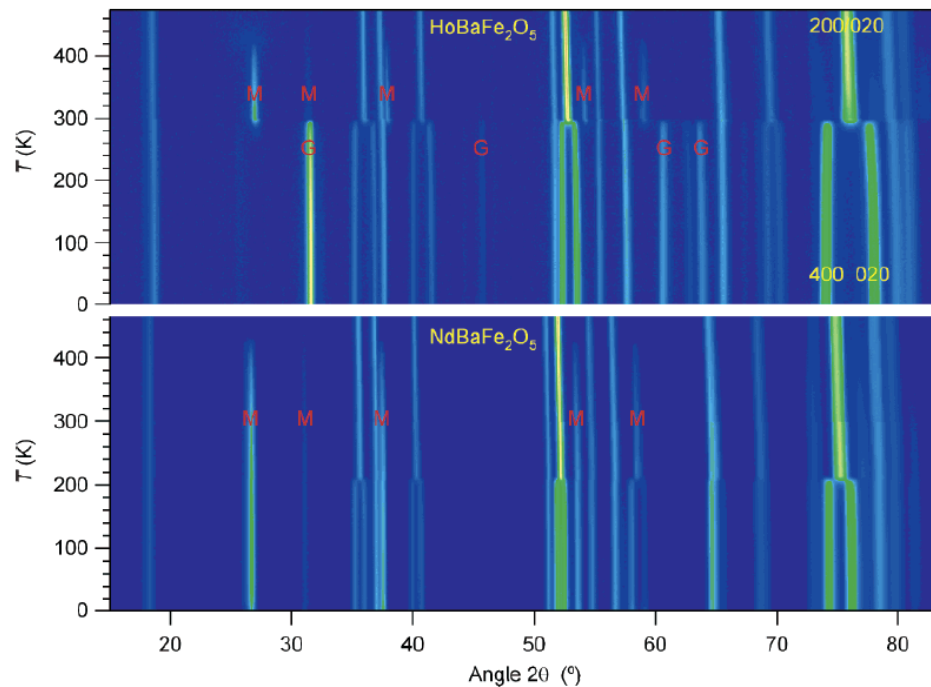


FIG. 9. CCD image of Fe_3Al powder (a) taken with stationary sample and (b) taken with sample rotation.

- Powder diffraction is excellent for getting the “big picture” but since intensities are spread over a sphere, small (but perhaps important) details are missed.
- Lose information about anisotropy

Thermodiffractometry

Detailed parameter dependence



High-flux mode leads
to high data rates

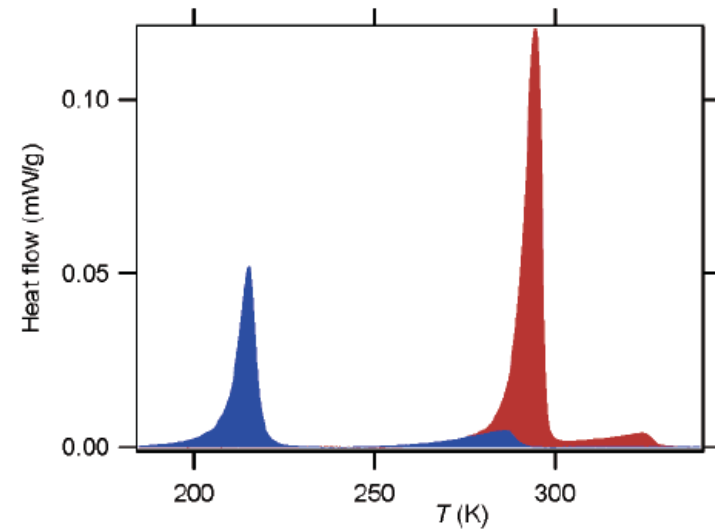
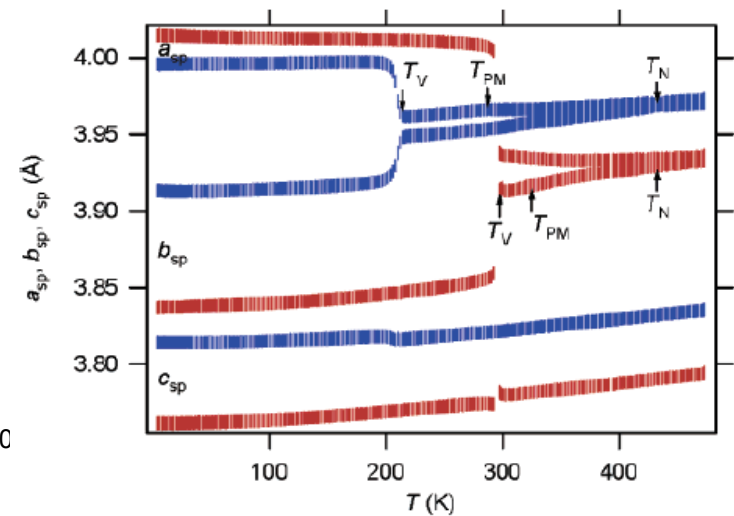


Figure 2. DSC peaks for NdBaFe₂O₅ (blue) and HoBaFe₂O₅ (red) upon heating. Areas give latent heat (ΔH) of the charge-ice melting.



Single-crystal diffraction

Single-crystal: more detail than powders
Wide angle diffraction: Get an overview of everything

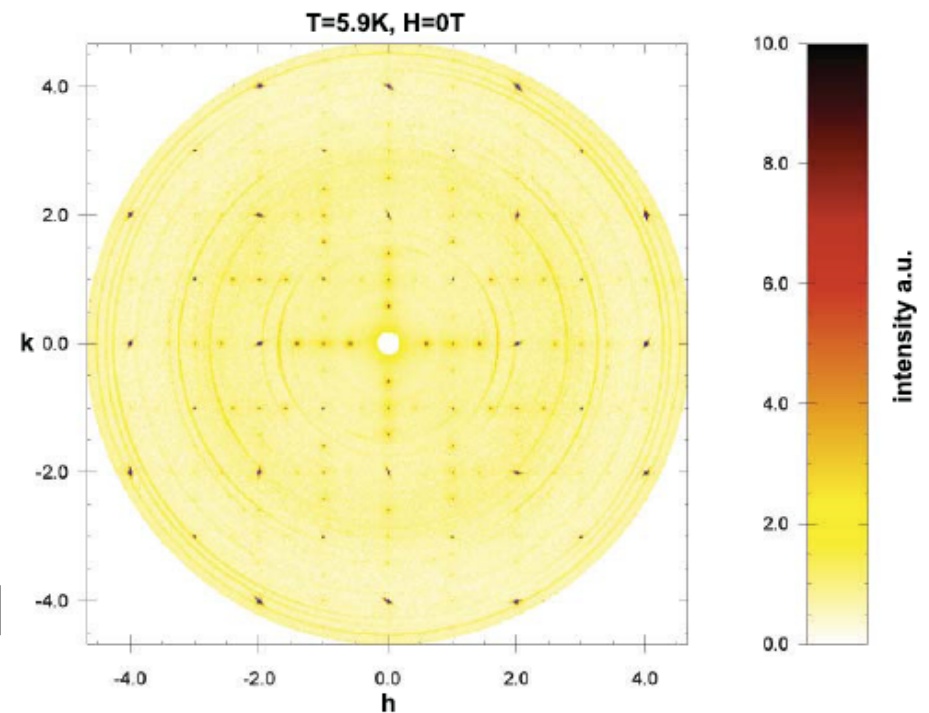
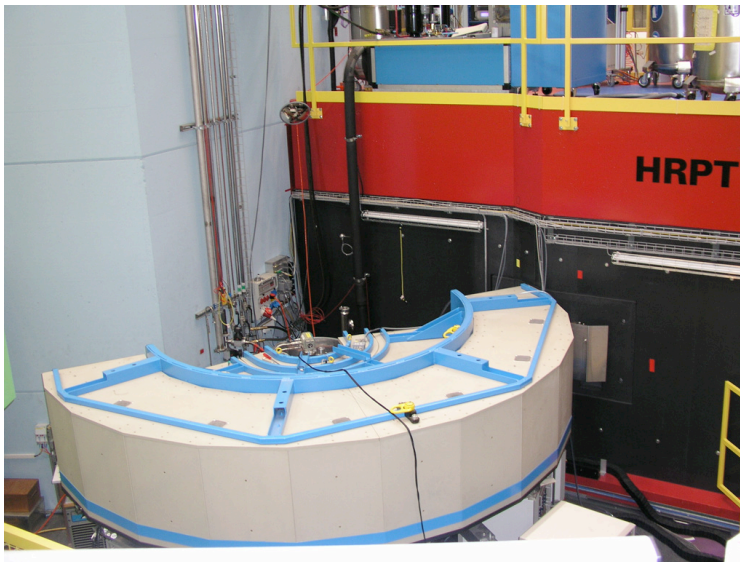
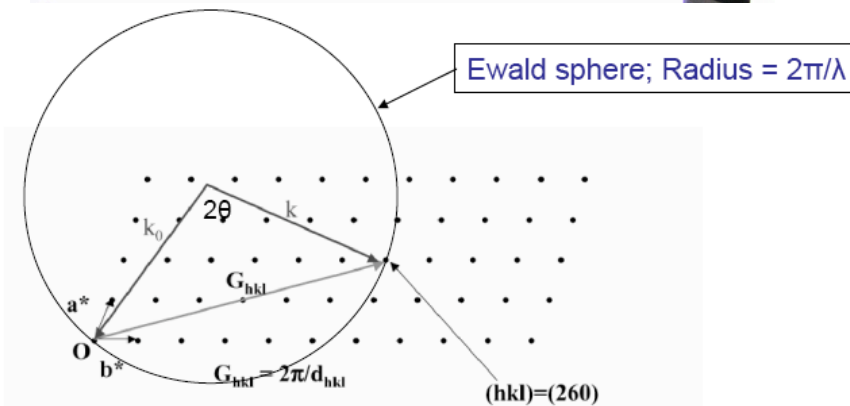
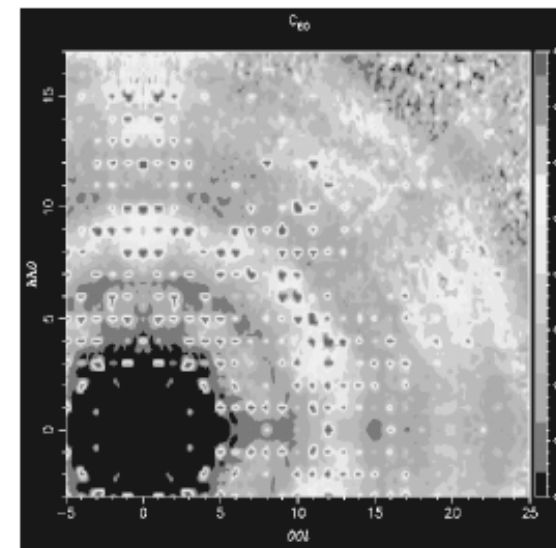
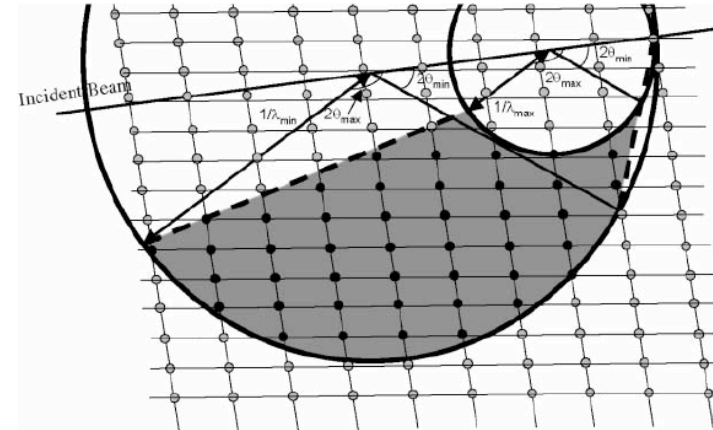


Figure 2: $\text{HoNi}_2\text{B}_2\text{C}$ single-crystal measured on HRPT

Incommensurate magnetism



TOF single-xtal diffraction

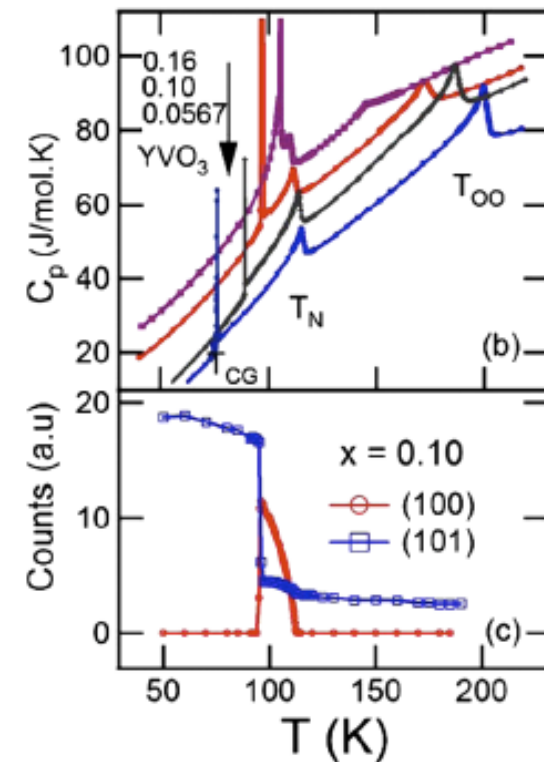
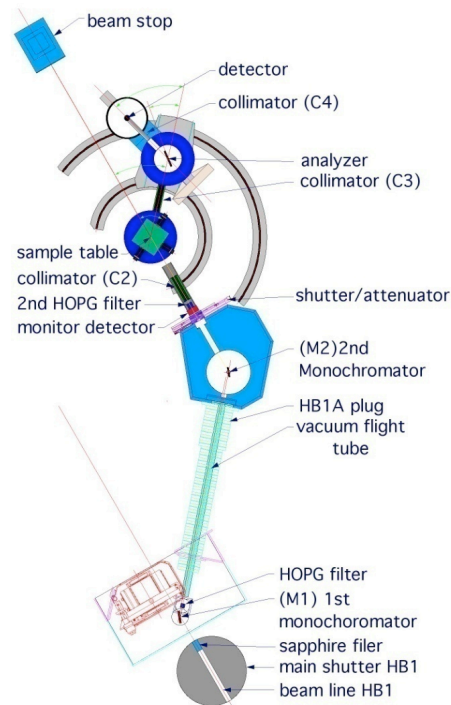


Single crystal diffraction

Triple-axis diffraction: focus in on specific points of interest



HB-1A 3-axis spectrometer



Orbital ordering in YVO_3

Further references

- **General neutron scattering**

- G. Squires, “Intro to theory of thermal neutron scattering”, Dover, 1978.
- S. Lovesey, “Theory of neutron scattering from condensed matter”, Oxford, 1984.
- R. Pynn, <http://www.mrl.ucsb.edu/~pynn/>.

- **Structural refinements**

- GSAS <http://www.ncnr.nist.gov/xtal/software/gsas.html>
- FullProf
<http://www.ill.eu/sites/fullprof/>

- **How to get beam time**

- Talk to one of us at Ames about your experiment
- We can identify a suitable instrument
- Talk to instrument scientist
- Write a beamtime request